What is Sound?

Music 171: Sinusoids

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- The word *sound* is used to describe both:
 - 1. an auditory sensation in the ear



2. the disturbance in a medium that causes an auditory sensation



- Nearly all objects will vibrate when disturbed.
- Sound is a **wave** created by vibrating objects.
 - alternating regions of low and high pressure that propagate through a medium from one location to another.

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Sound Wave

- Sound is a mechanical wave:
 - it requires a *medium* in which to propagate.
- Sound is a traveling wave:
 - it propagates from one location to another
- In fluids (air, water) sound is a **longitudinal** wave (has alternating regions of low and hight pressure).



• The **waveform** illustrates the *pressure variation* (either temporal or spatial) of the wave.

Waveform: wavelength

- The **wavelength** is the *length* of one **cycle**:
 - distance between crests or between troughs



• Waves are often characterized by their length:



- infrasonic: lower than lowest audible frequency.
- ultrasonic: higher than highest audible frequency.

Waveform: period/frequency

• Waves may also be characterized by their period and/or frequency.

• The **period** is the *time* to complete one cycle:



• If we know wave velocity, we can determine the period from the wavelength:

$$period = \frac{wavelength}{velocity}$$

- The frequency is:
 - the number of cycles per second (Hz)
 - inverse of the period

$$\mathsf{frequency} = \frac{1}{\mathsf{period}} = \frac{\mathsf{velocity}}{\mathsf{wavelength}}$$

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Properties of Sound Waves

• Speed of sound¹:

 $- \mbox{ in air: } 340 \mbox{ m/s}$

- $\mbox{ in water: } 1480 \mbox{ m/s}$
- Amplitude range of hearing (humans)
 - Threshold of audibility: 0.00002 Pa
 - Threshold of feeling (or pain!): 200 Pa
- Frequency range of hearing
 - $-\ humans:\ 20$ 20 000 Hz
 - $-\mbox{ dogs: } 20$ 45 000 Hz
 - beluga whale: 1000 123 000 Hz
- Period of lowest and highest audible frequencies

$$-1/20 \text{ Hz} = 0.05 \text{ s}$$
 $1/20 \ 000 \text{ Hz} = 0.05 \text{ ms}$

- Shortest human audible wave (air)
 - 340/20000=1.7cm
- Longest human audible wave (air)
 - -340/20 = 17 m

¹Quantity depends on temperature: For air, the speed of sound is $c = 20.1\sqrt{T}$, where T is the absolute temperature found by adding 273 to the temperature on the Celsius scale.

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- The *temporal waveform* of the sound shows the time evolution of the *pressure* variations, illustrating:
 - **amplitude**: maximum particle displacement from rest position (Pa).
 - **period**: time to complete one cycle (s).
 - **frequency**: number of cycles per second (Hz).
 - wavelength: length of one complete cylce (m) (need wave speed to compute).

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Why Sinusoids are Important

- Sinusoids are fundamental in physics: many systems oscillate in a quasi-sinusoidal motion known as **simple harmonic motion**:
 - repetitive movement through an equilibrium position
 - maximum displacement on either side of equilibrium is equal (if no losses).



 Sound is *bandlimited* and may be approximated by the sum of sinusoids (having frequencies up to a maximum value). 6

Sinusoids

Cycle and (Initial) Phase

• "Sinusoids" may be represented using both sine and cosine functions having the form:

 $x(t) = A\sin(\omega t + \phi)$ or $x(t) = A\cos(\omega t + \phi)$,

where x(t) is the quantity that varies over time and

- $A \triangleq$ peak amplitude
- $\omega \triangleq$ radian frequency $(rad/sec) = 2\pi f$
- $f \triangleq$ frequency (Hz)
- $t \triangleq \text{time (seconds)}$
- $\phi \triangleq$ initial phase (radians)



- \bullet One ${\rm cycle}$ of a sinusoid is 2π radians.
- The **phase** refers to the position within the cycle and is dependent on whether using a

1. sine function $(\sin(\omega t))$:



2. or a cosine function $(\cos(\omega t))$:



• The **initial phase** is the phase at time = 0 and is

 $-\pi < \phi < \pi, \quad \text{or} \quad 0 < \phi < 2\pi.$

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Initial Phase

- The **initial phase** ϕ (or *phase offset*), in radians, gives the position of the waveform cycle at t = 0.
- Sine function with $\phi = 0$ (sin($\omega_0 t + 0$)):



• Sine function with $\phi = \pi/2 \left(\sin(\omega_0 t + \pi/2) \right)$:



• ... or equivalently $\cos(\omega_0 t + 0)$.

Frequency (Hz vs. Rad/s)

- The frequency *f* of the waveform is given in cycles per second or Hertz (Hz).
- \bullet Frequency is equivalent to the inverse of the period T of the waveform,

$$f = 1/T$$
 Hz

• The radian frequency ω , given in radians per second, is equivalent to the frequency in Hertz scaled by 2π ,

$$\omega = 2\pi f \quad (rad/sec)$$

• What is the frequency in Hz of the following sinusoid?



• What is the frequency in rad/sec?

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Sine and Cosine Functions

• The sine and cosine function are very closely related and can be made equivalent simply by adjusting their initial phase:



Figure 2: Phase relationship between cosine (solid blue line) and sine (broked green line) functions.

Time (s)

0.5 0.6 Time (s)

0.5 Time (s)

Figure 3: A sinusoid with an amplitude envelope.

Steady State

Amplitude Envelopes

- In his work, *On the Sensations of Tone*, Hermann von Helmholtz characterized tones by the way in which their amplitudes evolved over time, that is, by their *amplitude envelope*.
- He described the envelope as having three parts:
 - 1. **the attack**: the time it takes the sound to rise to its peak
 - 2. **the sustain**: the steady state portion of the sound (where the amplitude has negligiable chane)
 - 3. **the decay**: the time it take for the sound to decay or fade out.

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ADSR Envelope

- The duration of the attack and decay greatly influence the quality of a tone:
 - wind instruments tend to have long attacks, while percussion instruments tend to have short attacks.
- Another envelope, called ADSR, has a fourth segment inserted between the attack and the sustain.
 - A: Attack
 - **D**: Decay
 - **S**: Sustain
 - $-\mathbf{R}$: Release



• The ADSR attempts to mimic envelopes found in musical instrument tones.



Dec

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Amplitude

Amplitude

Amplitude

0.5

-0.5

Attack

0